



2006



**MATHEMATICS COLLOQUIUM SERIES**  
**UNIVERSITY OF CENTRAL FLORIDA**

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OF

Illinois Wesleyan University

will speak on

Inversion Formulas and Their Applications

Here we present several inversion formulas and their applications in the expansion and interpolation problems. First, the concept of a generalized Stirling number pair can be characterized by a pair of inverse relations, in which the problem of expansion of  $A(t)f(g(t))$  (a composition of any given formal power series) can be constructively solved with the aid of Sheffer-type differential operators. Using the generalized Stirling number pair, we establish an inversion formula that can be applied to find an expansion of an analytic function  $f$  in terms of a sequence of Sheffer-type polynomials  $\{p_n\}$ . The result can be readily extended to the higher dimensional setting.

Secondly, multivariate rational exponential Lagrange interpolation formulas, Hermite interpolation formulas, and Hermite-Fejer interpolation formulas of the Newton type are established by using Carlita's inversion formulas. By setting  $q$  to 1, the obtained formulas are reduced to the corresponding multivariate polynomial interpolation formulas with combinatorial form.

Finally, we provide a wide class of Mobius inversion formulas in terms of the generalized Mobius functions and its application to the setting of the Selberg multiplicative functions.

**DATE: Tuesday, March 7, 2006**  
**TIME: 11:30 A.M. – 12:20 P.M.**  
**PLACE: Math and Physics Building, Room 233**